

Recall our new derivative formula from Section 5.1:

Parallel Integration Formula:

-example- Evaluate each integral.

1.  $\int (2x + 3 - \frac{5}{x} + \frac{6}{\sqrt{x}}) dx$

2.  $\int \frac{1}{4x-1} dx$

3.  $\int \frac{t}{t^2+5} dt$

4.  $\int \frac{1}{5-y} dy$

\*4. IMPROPER FRACTION:  $\int \frac{x^2 + 1}{x + 1} dx$

5.  $\int \tan x dx$

\*New Trig Integration Formulas: (**MEMORIZE THESE!**)

$$\int \tan u du$$

$$\int \cot u du$$

$$\int \sec u du$$

$$\int \csc u du$$

-examples- Evaluate each DEFINITE integral

$$1. \int_{\pi/4}^{\pi/2} \cot x dx$$

$$2. \int_0^{\pi/2} \sec\left(\frac{1}{2}x\right) dx$$

$$3. \int_1^e \frac{\ln^3 x}{x} dx$$

APPLICATIONS:

1. Find the area of the region enclosed by the function  $f(x) = \frac{2}{x \ln x}$ , the  $x$ -axis, and the vertical lines  $x = 2$  and  $x = 4$ .

2. Find the AVERAGE VALUE of the function  $f(x) = \frac{8}{3-2x}$  on the interval  $[-2, 1]$ .

3. Solve the differential equation:  $\frac{dy}{dx} = \tan 2x$ , given that  $y(0) = 2$

**SUMMARY of Derivative and Integral Formulas**

Derivatives:

$\frac{d}{dx} u^n =$
$\frac{d}{dx} (\ln u) =$
$\frac{d}{dx} (\sin u) =$
$\frac{d}{dx} (\cos u) =$
$\frac{d}{dx} (\tan u) =$
$\frac{d}{dx} (\cot u) =$
$\frac{d}{dx} (\sec u) =$
$\frac{d}{dx} (\csc u) =$

Integrals:

1.  $\int u^n du =$

7.  $\int \tan u \sec u du =$

2.  $\int \frac{1}{u} du =$

8.  $\int \cot u \csc u du =$

3.  $\int \sin u du =$

9.  $\int \tan u du =$

4.  $\int \cos u du =$

10.  $\int \cot u du =$

5.  $\int \sec^2 u du =$

11.  $\int \sec u du =$

6.  $\int \csc^2 u du =$

12.  $\int \csc u du =$